

# Could making banks hold only liquid assets induce bank runs?

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# Agenda

- Contextualization
- Model: assumptions (vs Diamond-Dybvig)
- Banks (unified and separated system)
- Welfare maximization problem
- Results
- Take-aways

# Contextualization

- Glass-Steagall Act (Banking Act of 1933)

*“To provide for the **safer and more effective** use of the assets of banks, to regulate interbank control, to prevent the undue diversion of funds into speculative operations [...] .”*

- Repeal of Glass-Steagall Act (1999)

# Is Glass-Steagall's repeal to blame?

- Paul Volcker (March 2009)

*"Maybe we ought to have a **two-tier financial system.**"*

*"This institutions should not be taking extraordinary risks in the market place represented by hedge funds, equity funds, large-scale proprietary trading. Those things would put their basic functions in jeopardy"*

- Could making banks hold only liquid assets induce bank runs? (PS, April 2010)

# Model

- 3 periods:  $T = 0$      $T = 1$      $T = 2$
- Continuum of consumers:  $[0; 1]$
- Single good (costless storage)
- Each endowed with  $y$  in  $T = 0$

# Model

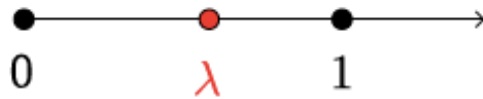
- In  $T = 0$  each consumer is identical
- In  $T = 1$  they discover their type (patient or impatient)
- Private information
- Sequential service constraint
- Until now, same assumptions as in Diamond and Dybvig (1983)

# Model

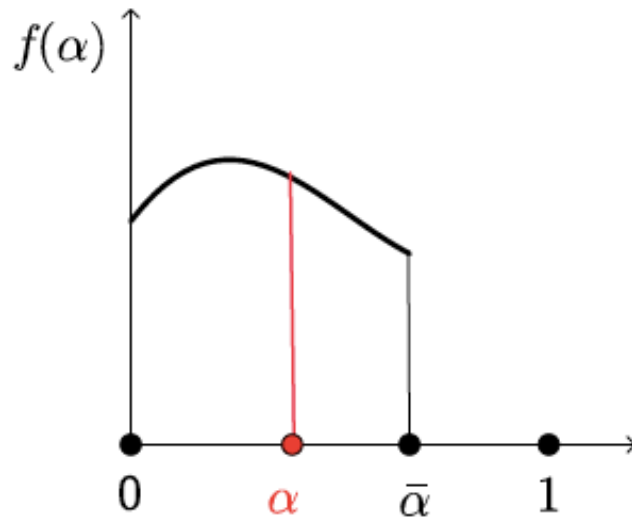
- $\alpha$  : probability of being impatient
- $\alpha$  is a random variable with density  $f$
- Support:  $[0, \bar{\alpha}]$        $\bar{\alpha} < 1$
- $\bar{\alpha}$ : maximum proportion of impatient consumers

# What is the difference?

Diamond-Dybvig



Peck-Shell



Intrinsic uncertainty



# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

# The utility functions

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$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

$C_I^1$ : consumption available to an impatient in  $T = 1$

# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

$C_P^1$ : consumption available to a patient in  $T = 1$

# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

$C_I^2$ : consumption available to an impatient in  $T = 2$

# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

$C_P^2$ : consumption available to a patient in  $T = 2$

# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

$$U_P(C_P^1, C_P^2) = \bar{u} + u(C_P^1 + C_P^2 - 1)$$

$\bar{u}$  : incremental utility of:

- 1 unit of consumption in  $T = 1$  for an impatient
- 1 unit of consumption in  $T = 2$  for a patient

# The utility functions

$$U_I(C_I^1, C_I^2) = \begin{cases} \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 \geq 1 \\ \beta \bar{u} + u(C_I^1 + C_I^2 - 1) & \text{if } C_I^1 < 1 \end{cases}$$

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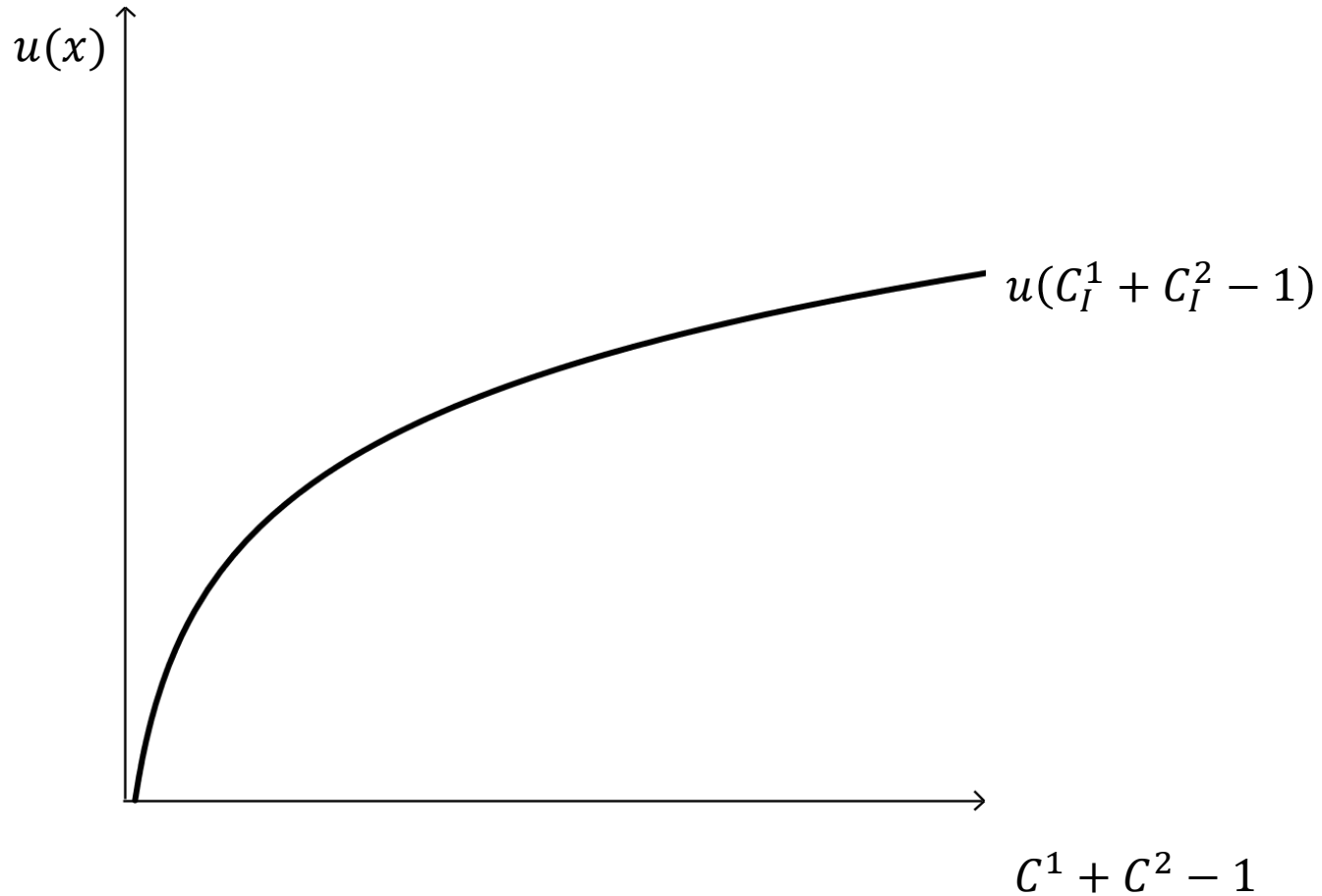
$\beta \bar{u}$ : incremental utility of 1 unit of consumption in  $T = 2$  for an impatient

# The utility functions

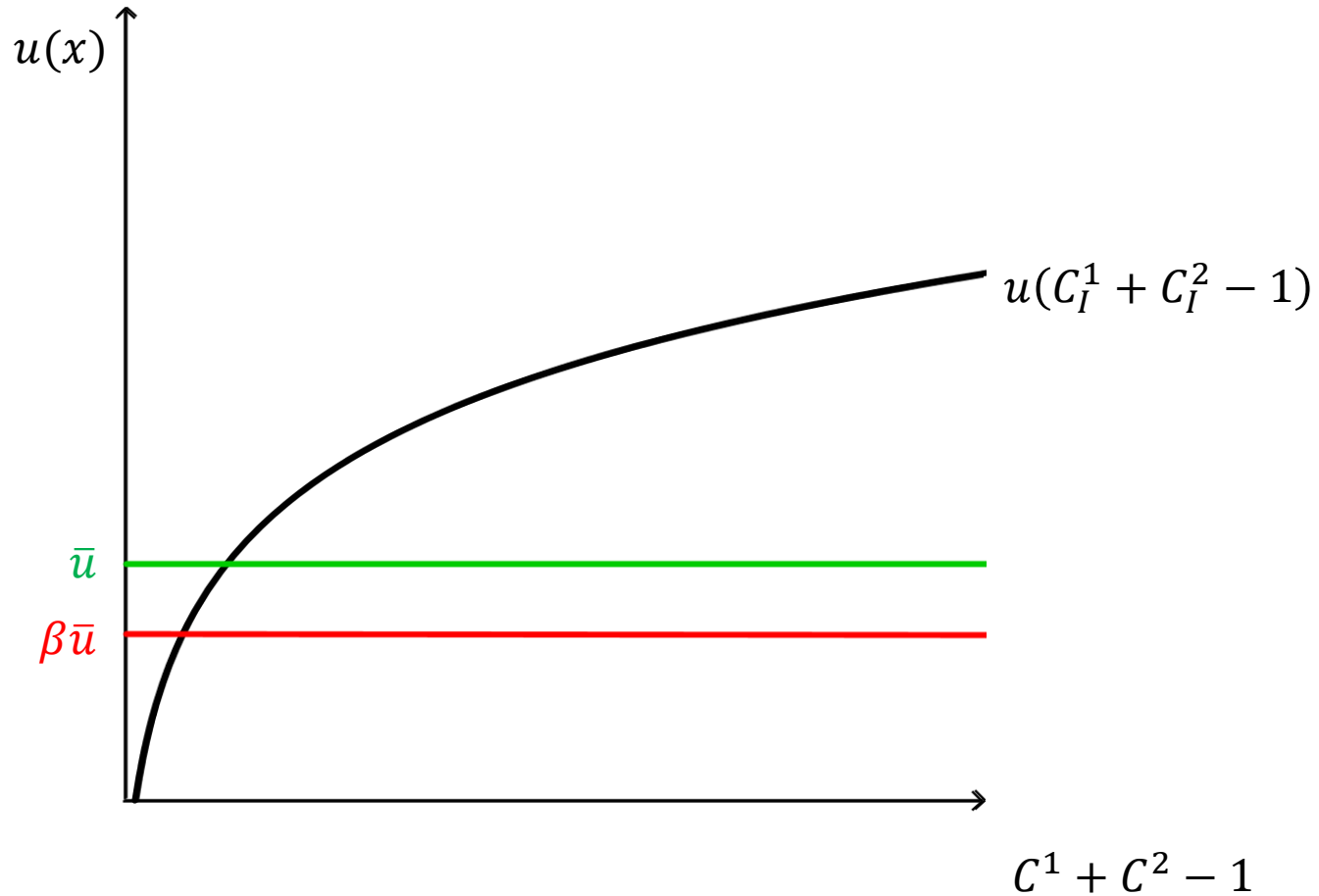
$u(C^1 + C^2 - 1)$ : utility from “*left-over*” consumption



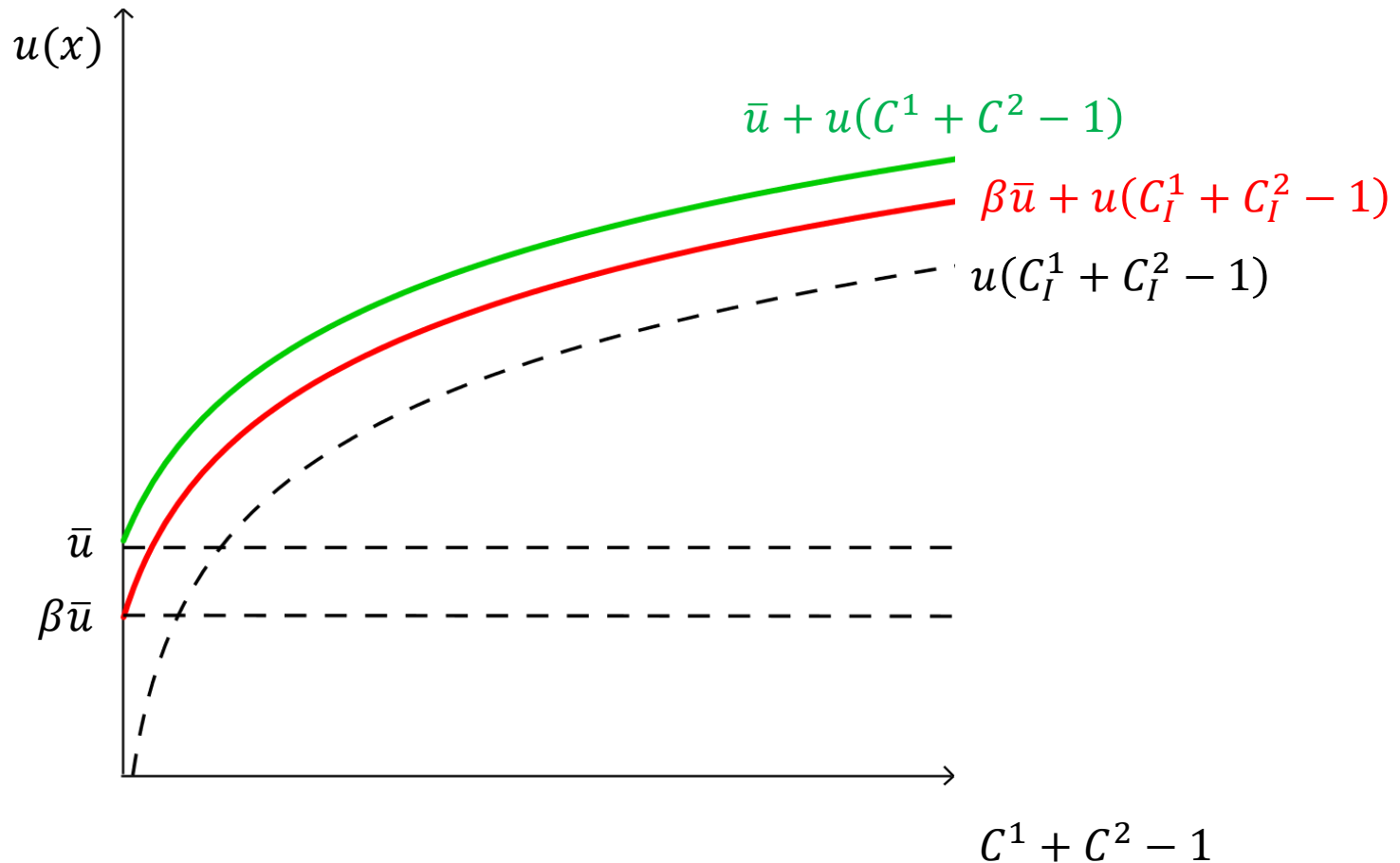
# The utility functions



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# The utility functions





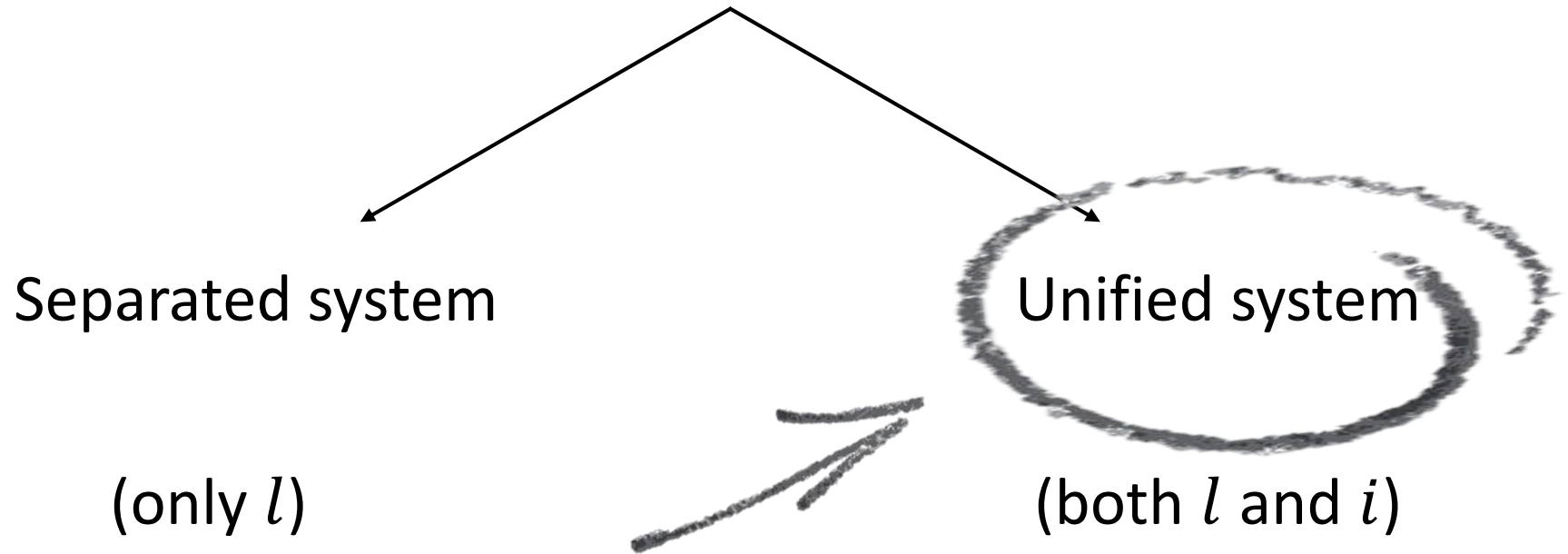
# Recap (What's new?)

- $\alpha \sim f_\alpha(\alpha) * 1_{[0, \bar{\alpha}]}(\alpha)$

- $U(x) = \frac{\bar{u}}{\beta \bar{u}} \text{ or } + u(C^1 + C^2 - 1)$

- $i$  (illiquid) returns  $R_i$  in  $T = 2$
- $l$  (liquid) returns  $R_l$  in  $T = 2$

# Banks



# Contract

$$\text{specifies } \begin{cases} \gamma \\ c^1(z) \\ c_I^2(\alpha_1) \\ c_P^2(\alpha_1) \end{cases}$$

$\gamma =$  % of endowment in  $l$

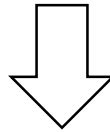
$c^1(z) =$  withdrawal in  $T = 1$

$c_I^2(\alpha_1) =$  withdrawal in  $T = 2$  if he also withdrew in  $T = 1$

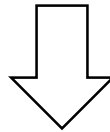
$c_P^2(\alpha_1) =$  withdrawal in  $T = 2$  if he did not withdraw  
in  $T = 1$

# Welfare

No entry costs



Perfect competition



**Maximize utility**

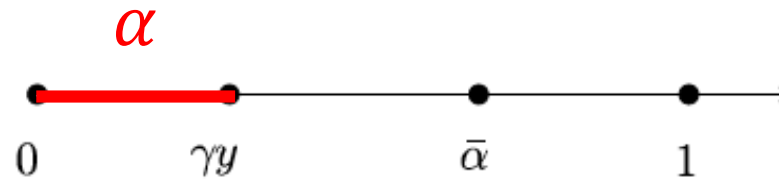


# Welfare

Remarks:

- $c^1(z) = 1$                       Maximum withdrawal in  $T = 1$
- $\gamma y \leq \bar{\alpha} * 1$                       Maximum investment in  $l$

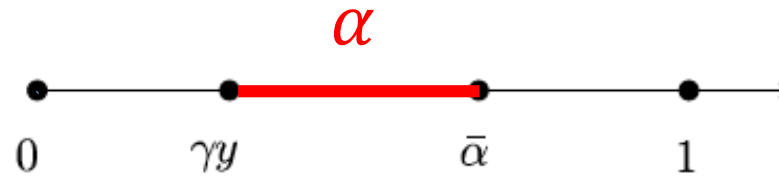
# Welfare



- $\alpha \leq \gamma y$

All impatient agents satisfied

# Welfare



- $\alpha \leq \gamma y$  All impatient agents satisfied
- $\alpha > \gamma y$  Only  $\gamma y$  impatient agents satisfied

# Welfare

$$\begin{aligned} W = & \int_0^{\gamma y} \left[ \bar{u} + (1 - \alpha)u \left( (1 - \gamma)yR_i + c_P^2(\alpha) - 1 \right) + \alpha u \left( (1 - \gamma)yR_i + c_I^2(\alpha) \right) \right] f(\alpha) d\alpha + \\ & + \int_{\gamma y}^{\bar{\alpha}} \left[ (1 - \alpha + \gamma y)\bar{u} + (\alpha - \gamma y)\beta\bar{u} + (1 - \alpha)u \left( (1 - \gamma)yR_i + c_P^2(\alpha) - 1 \right) + \right. \\ & \left. + (\alpha - \gamma y)u \left( (1 - \gamma)yR_i + c_P^2(\alpha) - 1 \right) + \gamma y u \left( (1 - \gamma)yR_i + c_I^2(\alpha) \right) \right] f(\alpha) d\alpha \end{aligned}$$

# Welfare

**Nobody is rationed**

$$\int_0^{\gamma y} \{\alpha[\bar{u} + u(C_I^T)] + (1 - \alpha)[\bar{u} + u(C_P^T)]\} f(\alpha) d\alpha$$

$\alpha[\bar{u} + u(C_I^T)] :$  utility of all impatient agents

$(1 - \alpha)[\bar{u} + u(C_P^T)] :$  utility of all patient agents

# Welfare

**$(\alpha - \gamma y)$  are rationed**

$$\int_{\gamma y}^{\bar{\alpha}} \{ \gamma y [\bar{u} + u(C_I^T)] + (1 - \alpha) [\bar{u} + u(C_P^T)] + (\alpha - \gamma y) [\beta \bar{u} + u(C_P^T)] \} f(\alpha) d\alpha$$

$$\gamma y [\bar{u} + u(C_I^T)] :$$

utility of all satisfied impatient agents

$$(1 - \alpha) [\bar{u} + u(C_P^T)] :$$

utility of all patient agents

$$(\alpha - \gamma y) [\beta \bar{u} + u(C_P^T)] :$$

utility of all rationed impatient agents

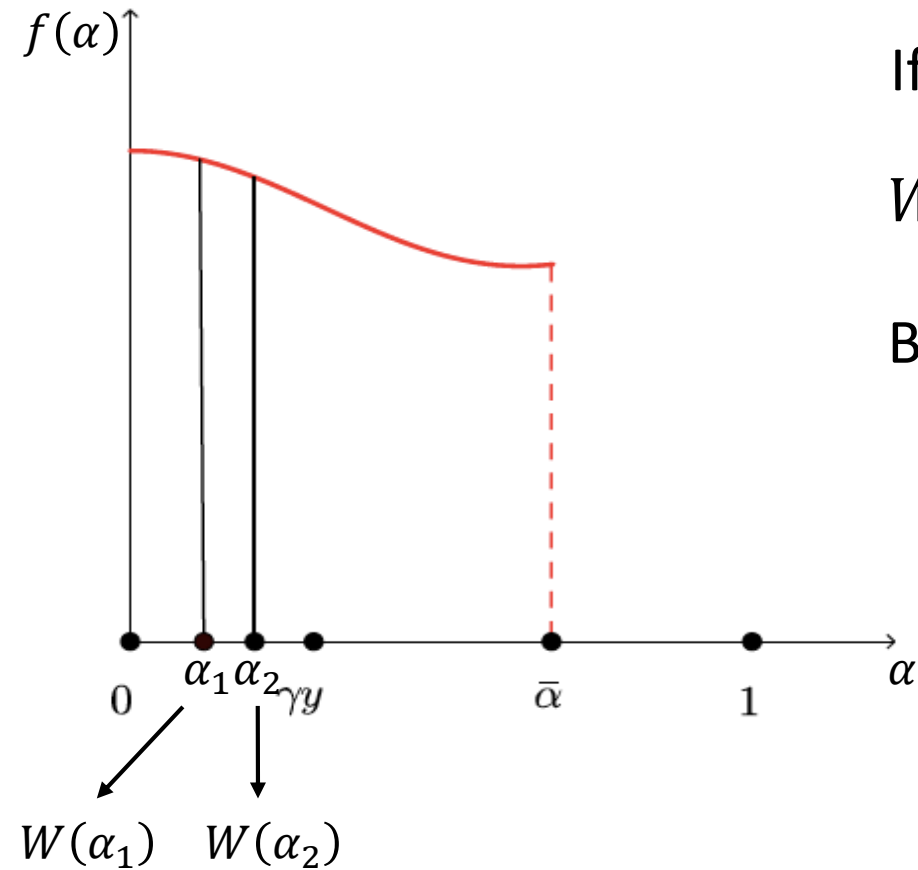
# Welfare

If it was discrete:

$$W = W(\alpha_1)P(\alpha_1) + W(\alpha_2)P(\alpha_2) + \dots$$

But it is continuous:

$$W = \int_0^{\alpha} \{ \dots \} f(\alpha) d\alpha$$



# Constraints

## Resource constraint (only $l$ )

$$\alpha_1 c_I^2(\alpha_1) + (1 - \alpha_1) c_P^2(\alpha_1) = (\gamma y - \alpha_1) R_l \quad \alpha_1 \leq \gamma y$$

$$\gamma y c_I^2(\alpha_1) + (1 - \gamma y) c_P^2(\alpha_1) = 0 \quad \alpha_1 > \gamma y$$



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LHS: amount of withdrawals in  $T = 2$

RHS: resources that can be withdrawn in  $T = 2$

# Constraints

## Resource constraint (only $l$ )

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$$\gamma y c_I^2(\alpha_1) + (1 - \gamma y) c_P^2(\alpha_1) = 0 \quad \alpha_1 > \gamma y$$

$\alpha_1 c_I^2(\alpha_1)$ : withdrawals of impatient agents in  $T = 2$

$(1 - \alpha_1) c_P^2(\alpha_1)$ : withdrawals of patient agents in  $T = 2$

# Constraints

## Resource constraint (only $l$ )

$$\alpha_1 c_I^2(\alpha_1) + (1 - \alpha_1) c_P^2(\alpha_1) = (\gamma y - \alpha_1) R_l \quad \alpha_1 \leq \gamma y$$

$$\gamma y c_I^2(\alpha_1) + (1 - \gamma y) c_P^2(\alpha_1) = 0 \quad \alpha_1 > \gamma y$$

$\gamma y c_I^2(\alpha_1)$ : withdrawals of satisfied impatient agents  
in  $T = 2$

$(1 - \gamma y) c_P^2(\alpha_1)$ : withdrawals in  $T = 2$  of who did not  
withdrawn in  $T = 1$

# Constraints

## Resource constraint (only $l$ )

$$\alpha_1 c_I^2(\alpha_1) + (1 - \alpha_1) c_P^2(\alpha_1) = (\gamma y - \alpha_1) R_l \quad \alpha_1 \leq \gamma y$$

$$\gamma y c_I^2(\alpha_1) + (1 - \gamma y) c_P^2(\alpha_1) = 0 \quad \alpha_1 > \gamma y$$

$\gamma y$  : total  $l$  invested

$\alpha_1 \cdot 1$ : total amount of withdrawals of impatient agents  
in  $T = 1$

$R_l$ : returns on asset  $l$

# Constraints

## Incentive compatibility constraint

$$\int_0^{\bar{\alpha}} u(C_P^2) f_p(\alpha) d\alpha \geq \int_0^{\bar{\alpha}} u(C_I^2) f_p(\alpha) d\alpha$$

# Constraints

## Incentive compatibility constraint

$$\int_0^{\bar{\alpha}} u(C_P^2) f_p(\alpha) d\alpha \geq \int_0^{\bar{\alpha}} u(C_I^2) f_p(\alpha) d\alpha$$

$u(C_P^2)$  = expected utility of a patient that does not withdraw in  $T = 1$

$u(C_I^2)$  = expected utility of a patient that withdraws in  $T = 1$

$f_p(\alpha)$  = density of  $\alpha$  from a patient consumer's point of view

# Maximization problem

$$\begin{aligned} & \max && W \\ & \gamma, c_I^2(\alpha_1), c_P^2(\alpha_1) \\ & s. t. && (ICC) \text{ and } (RC) \end{aligned}$$

# Results

## THEOREM 3.1

A bank will never invest more than  $\bar{\alpha}$  in  $l$  and there is full consumption smoothing

i)  $c_I^2(\alpha_1) = c_P^2(\alpha_1) - 1$

ii) Optimal contract  $\implies \gamma y < \bar{\alpha}$



# Results

## PROOF

i) Maximizing  $W$  sub. only to the RC, we obtain:

$$c_I^2(\alpha_1) = c_P^2(\alpha_1) - 1 \iff \text{Consumption Smoothing} \\ (\text{i.e. } C_P^{TOT} = C_I^{TOT})$$

Now,

$$\begin{cases} \text{RC} \\ \text{C.S.} \end{cases} \implies \text{ICC}$$

# Results

## PROOF

ii) Plugging RC and C.S. conditions in  $W$

$$\left(\frac{\partial W}{\partial \gamma}\right)_{\gamma=\bar{\alpha}/y} < 0$$

Investing more than  $\bar{\alpha}$  in  $l$  is sub-optimal

# Results

## **THEOREM 3.2**

- i) There exists an optimal contract for the unified bank, also socially optimal
  
  
  
  
  
  
  
  
  
  
- ii) Assuming that a patient does not run if indifferent,

$$C_P^{TOT} = C_I^{TOT} \implies \text{NO RUN}$$

# Results

## PROOF

i) Setting the RC and the C.S. to hold is sufficient for

$\max_{\gamma, c_I^2(\alpha_1), c_P^2(\alpha_1)} W$  to have a solution

- ii) • Under the optimal contract  $C_P^{TOT} = C_I^{TOT}$
- Patient agents are indifferent between running and not running

$\implies$  No run equilibrium

# Take-aways

- *“The unified system optimally resolves the trade-off between liquidity and economic growth; in doing so it maximizes social welfare”*
- *“Our Analysis in its present state does not prove that imposing Glass-Steagall restrictions would be a mistake, although it does suggest that one should be skeptical about the purported stability benefits. Before using the model to offer policy advise, moral hazard should be included.”*

# Sources

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